

# Index

The capsule symbol used throughout this book (a boldface numeral within brackets) appears again in the index. When an entry is the subject of an entire capsule, the symbol for that capsule precedes the listing of pages.

Pronunciations are given for certain words, usually personal names, where such guidance might prove helpful. The symbols used are the familiar diacritical marks used in *Webster's Biographical Dictionary* and in most older dictionaries (such as *Webster's New International Dictionary*, 2d ed., and *Webster's New Collegiate Dictionary*, 6th ed.).

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